measured from 15 to 300°K. A maximum occurs in the heat capacity at $216.1 \pm 0.5^{\circ}$ K. The heat of transition is 220 ± 15 cal. mole⁻¹ and the corresponding entropy change is 1.02 ± 0.07 cal. deg.⁻¹ mole⁻¹. The entropy of crystalline NH₄-

 H_2AsO_4 at 298.19°K. is 41.12 = 0.10 cal. deg.⁻¹ mole⁻¹. The transition is attributed to a rearrangement of the hydrogen bonds in the crystal. CAMBRIDGE, MASS.

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[CONTRIBUTION FROM THE RESEARCH LABORATORY OF PHYSICAL CHEMISTRY, MASSACHUSETTS INSTITUTE OF TECH-NOLOGY, NO. 501]

The Heat Capacity of Silver Trihydrogen Paraperiodate from 15 to 300°K. The Anomaly at the Curie Temperature

By C. C. Stephenson and H. E. Adams¹

The application of the third law of thermodynamics to compounds containing hydrogen bonds is a complicated problem. A residual entropy associated with a random orientation of the hydrogen bonds may persist to the lowest attainable temperatures, as in ice,1a heavy ice2 and sodium sulfate decahydrate.³ If the crystal structure of the compound is known in detail this residual entropy may be calculated, and Pauling⁴ has discussed a number of such cases. The experimental data required to confirm the predictions of theory have been obtained only for water and heavy water. However, in the compounds KH2-PO₄,⁵ KH₂AsO₄,⁶ and NH₄H₂PO₄,⁷ the transition from the random to an orientated arrangement of the hydrogen bonds occurs at easily attainable temperatures and the entropy of transiton may be measured directly. This entropy change may be calculated by Pauling's method or by the alternative method of Slater⁸; the two calculations give the same result for the total entropy change from the ordered to the disordered state. The good agreement between the theoretical and experimental values found in these cases justifies the application of the theory to other systems containing hydrogen bonds.

The structure⁹ of (NH₄)₂H₃IO₆ is very similar to the structure of KH₂PO₄ in so far as the hydrogen bonds are concerned, except that the octahedral IO₆ group is linked to neighboring paraperiodate groups by six hydrogen bonds, while the tetrahedral phosphate group has only four hydrogen bonds. In both cases the hydrogen bonds are unsymmetrically arranged around the central group and a preferred orientation of the hydrogens is possible at not too low a temperature. The

(4) I. Pauling, ibid., 57, 2680 (1935).

- (6) C. C. Stephenson and A. C. Zettlemoyer, ibid., 66, 1402 (1944).
- (7) C. C. Stephenson and A. C. Zettlemoyer, ibid., 66, 1405 (1944). (8) J. C. Slater, J. Chem. Phys., 9, 16 (1941).
- (9) L. Helmholz, THIS JOURNAL, 59, 2036 (1937)

expected transition was found¹⁰ in (NH₄)₂H₃IO₆ at 254°K., but the compound loses water and ammonia too rapidly to permit measurements on a sample of well-defined composition. The structurally similar salt, Ag₂H₃IO₆, was more suitable for accurate measurements from this point of view.

The heat capacity of silver trihydrogen paraperiodate has been measured from 15 to 300°K. The entropy of transition of this salt, estimated from the anomalous portion of the heat capacity curve, agrees satisfactorily with the predicted value of $3/4 R \ln 3$; this agreement is particularly gratifying as a test of the hydrogen bond theory in view of the comparatively large amount of entropy involved.

Material.—A number of silver periodates $(Ag_5IO_6, Ag_2H_3IO_6, Ag_3IO_5, Ag_2HIO_5, AgIO_4,$ and perhaps others) exist, and the preparation of pure Ag₂H₃IO₆ requires a careful control of temperature and concentration. As a starting point, Na₃H₂IO₆ is prepared by the oxidation of NaIO₃ with chlorine in a basic solution.¹¹ This salt is dissolved in dilute nitric acid and treated with a silver nitrate solution in the ratio of two moles of AgNO₃ to one of Na₃H₂IO₆. A finely divided greenish-yellow precipitate of Ag2H3IO6 is formed, but this precipitate usually changes into the red Ag₂HIO₅ with loss of water on standing for a day or more. A solution of 5N nitric acid is saturated with the salt at 80° (at this temperature all of the yellow salt is converted into Ag₂HIO₅), filtered at 40° to remove any AgIO₃ which has formed, and allowed to crystallize in an ice-bath. The solution is not heated above 80° because a white precipitate, presumably silver iodate, forms in larger amounts and the color of the solution turns to a deep brown. The solution can be filtered at 40° to remove this white precipitate since no more of it is formed at lower temperatures. The Ag₂H₃IO₆ forms so slowly that none starts to crystallize at this temperature, and it is usually necessary to allow the solution to crystallize for

(10) C. C. Stephenson, J. Chem. Phys., 9, 379 (1941).
(11) "Inorganic Syntheses," H. S. Booth, Editor-in-Chief, McGraw-Hill Book Company, Inc., New York, 1939, Vol. I, p. 169.

⁽¹⁾ Present address, Armstrong Cork Company, Lancaster, Pennsylvania.

⁽¹a) W. F. Giauque and J. W. Stont, THIS JOURNAL, 58, 1144 (1936).

⁽²⁾ E. A. Long and J. D. Kemp. ibid., 58, 1829 (1936).

⁽³⁾ K. S. Pitzer and I., V. Coulter, ibid., 60, 1310 (1938).

⁽⁵⁾ C. C. Stephenson and J. G. Hooley, ibid., 66, 1397 (1944).

twenty-four hours to ensure complete crystallization. The yields are about twenty grams of salt per liter of solution from the greenish-yellow precipitate, and considerably less from the red Ag_2HIO_5 or the black Ag_3IO_5 which eventually forms when the red salt is repeatedly heated with the acid solution. If the concentration of the nitric acid is increased, orange-yellow crystals of the tetragonal AgIO₄ are formed with a larger amount of the white silver iodate.

The silver trihydrogen paraperiodate crystallizes in beautifully formed yellow rhombohedra which sometimes grow to several millimeters on an edge. Some batches of the crystals were stable in air at room temperature for long periods of time, while other batches decomposed overnight into Ag₂HIO₅, but all of the batches remained undecomposed when kept in a refrigerator. The crystals dried rapidly in air and were further dried in vacuum for two hours without any signs of decomposition. Immediately after drying the salt in vacuum, the calorimeter was loaded and cooled below 0° within a few hours. The calorimeter was never allowed to rise above 0° until the final high temperature heat capacity measurements were made. The crystals were then removed from the calorimeter and examined for evidence of decomposition; the absence of any discoloration showed that no decomposition had occurred.

The rhombohedral angle for Ag₂H₃IO₆ is given by Groth¹² as 67°38'. The angle found for this preparation was 67°.18

The salt was analyzed quantitatively by three methods represented by the following equations:

 $\begin{array}{rl} 4Ag_{2}H_{3}IO_{6} &= 4AgI + 6H_{2}O + 9O_{2} + 4Ag\\ Ag_{2}H_{3}IO_{6} + 2HCI &= 2AgCI + H_{5}IO_{6}\\ 10Ag_{2}H_{3}IO_{6} + 12KOH &= 4Ag_{5}IO_{6} + 3K_{4}I_{2}O_{9} + 21H_{2}O \end{array}$

After heating Ag₂H₃IO₆ to constant weight at 400°, the loss in weight found in three experiments was 22.45, 22.44, and 22.43%; theoretical, 22.42%. When the salt was treated with 6Nnitric acid and hydrochloric acid, the decrease in weight on conversion to silver chloride was found to be 35.25, 34.98, and 35.01%; theoretical, 35.10%. When the salt was treated with potassium hydroxide and allowed to stand for five days, the decrease in weight on conversion to Ag₅IO₆ in two trials was 30.98 and 31.00%; theoretical, 30.97%. On the basis of these results, the sample used for the calorimetric measurements was 99.9% pure.

All of the measurements were made on a single loading of 464.227 g. in vacuum, or 1.0510 moles. These figures have been corrected for the presence of 0.053 weight per cent. of 10 mole per cent. nitric acid solution, as explained below. The molecular weight of $Ag_2H_3IO_6$ is taken as 441.704.

The density of the salt was needed to determine (12) Groth, "Handbuch der krystallographisch-physikalischen

Chemie," Leipzig, 1881, Vol. II, p. 181. (13) We wish to thank Dr. T. R. P. Gibb, Jr., Analytical Division of the Chemistry Department, M. I. T., for measuring this angle.

the volume of helium gas introduced into the calorimeter for heat conduction. The density of silver trihydrogen paraperiodate, found by displacement of water in a pycnometer, is 5.68 at 25-26°.

Apparatus and Method .- The cryostat used for these measurements has been described.14 This cryostat was adapted to calorimetric work by Dr. R. W. Blue. The calorimeter was the same as the one employed in the determination of the heat capacity of MnF_2 .¹⁵ The temperatures and

TABLE I

THE HEAT CAPACITY OF SILVER TRIHYDROGEN PARAPERIODATE

Molecular weight, 441.704; 0°C. = 273.19°K.

		Ср,			Ср,
Т . °К .	ΔT	mole ⁻¹	<i>Τ</i> , ⁰ Κ .	ΔT	cal. deg. ⁻¹ mole ⁻¹
	Series I		150.59	7.217	30.44
215.86	4.339	44.35	157.97	7.535	31.55
220.03	3.999	48.73	165.35	7.226	32.64
223.13	2.189	54.38	172.83	7.523	33.74
225.23	2.021	59.80	180.20	7.224	34.84
227.20	1.919	63.46	187.68	7.732	36.00
229.15	1.976	60.96	195.24	7.402	37.34
231.18	2.096	56.36	202.45	7.020	38.87
233.32	2.186	53.24	208.49	5.048	40.63
235.91	2.987	51,3 0	213.17	4.3 2 0	42.72
236.90	3.005	50.88		Series I	V
240.31	3.820	49.36	233.10	2.526	53.64
244.66	4.916	44.59	235.67	2.599	51.45
249.60	4.963	43.96	238.28	2.626	50.50
255.02	5.880	44.15	240.93	2.679	48.99
261.09	6.266	44.50	243.05	1.564	45.23
267.53	6.622	45.01	244.62	1.583	44.42
	Series II			Series V	7
223.70	2.867	55.67	15.31	0.644	2.086
225.74	1.212	61.03	16.19	1.150	2.342
226.43	0.176	62.55	17.84	2.335	2.839
226.61	0.176	62.62	20.09	2.563	3.566
226.78	0.176	62.43	22.94	3.153	4.557
226.99	0.234	63.00	26.70	4.377	5.792
227.28	0.349	63.49	31.10	4.330	7.245
227.71	0.518	63.36	35.26	3.991	8.562
228.28	0.628	62.62	39.43	4.335	9.800
229.01	0.838	60.78	44.13	5.076	11.12
\$	Series III	[49.01	4.673	12.45
72.82	6.861	17.74	54.08	5.484	13.68
79.39	6.256	18.95	59.68	5.713	14.99
85.75	6.482	20.12	65.45	5.822	16.27
92.02	6.043	21.23		Series V	I
98.19	6.297	22.31	23.46	2.865	4.725
104.60	6.520	23.37	26.61	3.616	5.743
110.68	5.648	24.37	\$	Series VI	I
116.54	6.058	25.31	270.32	8.245	45.25
122.77	6.414	26.29	278.49	8.091	45.96
129.34	6.733	27.27	286.74	8.432	46.61
136.22	7.015	28.29	295.08	8.242	47.29
143.35	7.258	29.35			

⁽¹⁴⁾ R. W. Blue and J. F. G. Hicks, THIS JOURNAL, 59, 1962 (1937).

⁽¹⁵⁾ J. W. Stout and H. E. Adams, ibid., 64, 1535 (1942).



energy inputs were measured by means of a platinum-rhodium resistance thermometer-heater having the laboratory designation R222. The ice-point resistance of this thermometer, which had been calibrated with a helium gas thermometer,¹⁴ agreed with the original calibration.

The calorie was taken to be 4.1833 international joules. The absolute temperature of the ice point was taken as 273.19°K.

Heat Capacity Measurements.-The results of the heat capacity measurements, obtained in seven series, are summarized in Table I, and presented graphically in Fig. 1. The correction for heat leak at the higher temperatures has been greatly reduced by the use of an adiabatic shield. Above 30°K., all of the experimental values fall within 0.1% of a smooth curve through the data except the very short runs in the transition region and one point which included the ice point. This value, at 270.32°K., was 0.60% high due to the condensation of water on the outside of the calorimeter. The cryostat developed a leak between Series VI and VII, and water condensed on the calorimeter in spite of a liquid nitrogen trap in the system. All of the values for this last Series VII have been corrected for 0.04 g. of water; the other measurements are, of course, unaffected. This correction amounts to 0.08% of the total heat capacity.

The peculiar shape of the heat capacity curve indicates the presence of two transitions superimposed upon each other. The short dotted

curve in Fig. 1 is an attempt to differentiate these two transitions. The secondary anomaly is undoubtedly caused by a small amount of nitric acid solution retained in the crystals in spite of the high vacuum to which they were subjected. According to the phase diagram for water and nitric acid,¹⁶ the melting of H₂O and HNO₈·3H₂O of a composition (10 mole % HNO₃) corresponding to that used for the recrystallization of the Ag₂H₃IO₆ would give an irregularity similar to that observed. It is unfortunate that the eutectic temperature of this mixture, 231°K., falls in the most interesting temperature range of these experiments. However, the changes in heat content and entropy for this secondary transition, estimated from the portion of the curve above the short dotted line in Fig. 1, are only 17.0 cal. mole⁻¹ and 0.07 cal. mole⁻¹ deg.⁻¹, respectively. This corresponds to 0.053% by weight of nitric acid solution impurity. Recently Forsythe and Giauque¹⁷ have published an extensive thermal study of nitric acid and its hydrates. Using their data on the heat capacity of HNO3.3H2O, combined with the data on the heat capacity of H₂O, ^{1a} it has been possible to correct our measurements for the presence of the nitric acid solution. The impurity was assumed to be composed of 0.00109 mole of HNO3·3H2O and 0.00654 mole

^{(16) &}quot;Gmelin's Handbuch der anorganischen Chemie," Systemnummer 4, Stickstoff, 8th edition, Berlin, 1936, p. 969.

⁽¹⁷⁾ W. R. Forsythe and W. F. Giauque, THIS JOURNAL. 64, 48 (1942).

of H₂O. The total correction amounted to 0.09-0.16% of the total heat capacity below the melting temperature range and 0.38-0.35% above the melting temperature range.

The results given in Table I are the original values of the heat capacity and have not been corrected for the presence of the nitric acid solution. However, the values at even temperatures listed in Table II were taken from a smooth curve through the data and have been corrected for the presence of the impurity. These values represent the true differential heat capacity and are believed to be accurate to 0.2% above 35° K., to 1% at 20° K., and to 5% at 15° K.

TABLE II

THE HEAT CAPACITY OF SILVER TRIHYDROGEN PARAPERIODATE

Values from a smooth curve through the observations.

	C.		Ca
Т, ° К .	cal. deg. ⁻¹ mole ⁻¹	Т, °К.	cal. deg. ⁻¹ mole ⁻¹
15	2.000	150	30.31
20	3.540	160	31.79
25	5.216	170	33.28
30	6.879	180	34.76
35	8.469	190	36.33
4 0	9.955	200	38.24
45	11.36	210	41.17
50	12.68	215	43.70
55	13.88	22 0	48.61
60	15.04	224	56.33
65	16.13	227.25	63.5 (max.)
70	17.15	230	58.89
75	18.12	234	52.04
80	19.05	238	48.08
85	19.95	242	45.37
90	20.84	245	44.17
95	21.72	250	43.79
100	22.57	260	44.26
110	24.23	270	45.05
120	25.80	280	45.90
130	27.33	290	46.71
140	28.82	30 0	47.48

Transition Temperature.—The abnormally high heat capacities from 180.0 to 268.5° K. are caused by the re-orientation of the hydrogen bonds in the solid. Although the transition occurs over a wide range of temperatures, it is customary to define the transition temperature as the temperature at which the heat capacity reaches a maximum. The maximum occurs at $227.25 \pm 0.20^{\circ}$ K.; this temperature is somewhat difficult to locate because the heat capacity curve is apparently dome-shaped near the peak.

Heat and Entropy of Transition.—The change in heat content, derived from the heat capacity curve, uncorrected for the presence of HNO_8 solution, is 3943.0 cal. mole⁻¹ from 180.0 to 268.5°K. The change in heat content from 180.0 to 268.5°K., assuming "normal" heat capacities in this temperature region, is 3567.9 cal. mole⁻¹. The heat of transition is then 375.1 \pm 20.0 cal. mole⁻¹. Corresponding figures for the entropy changes are: experimental, 17.65 e. u. from 180.0 to 268.5° K.: calculated for "normal" heat capacities, 15.98 e. u. from 180.0 to 268.5° K. The entropy change for the transition is then 1.67 ± 0.10 cal. deg.⁻¹ mole⁻¹.

If, however, the proper corrections for the presence of the nitric acid solution are made, the heat of transition and the entropy change for the hydrogen bond anomaly are then 358.1 ± 20.0 cal. mole⁻¹ and 1.60 ± 0.10 cal. mole⁻¹ deg.⁻¹.

cal. mole⁻¹ and 1.60 ± 0.10 cal. mole⁻¹ deg.⁻¹. **Entropy** of Ag₂H₃IO₆ at 298.19°K.—The entropy of the salt was determined by graphical integration of $\int C_p$ d ln T from 15 to 298.19°K. The entropy from 0 to 15°K. was obtained by means of a Debye function, 2D(112.2°K.) per mole of Ag₂H₃IO₆. Table III is a summary of the calculation. The correction due to the presence of the HNO₈ impurity is subtracted separately.

TABLE III

THE ENTROPY OF Ag2H3IO6

0–15°K., Debye extrapolation	0.71
15-298.19°K., graphical integration	58.95
	·····
	59. 66
Minus entropy due to HNO ₂ impurity	0.22
	59.44 ± 0.10 cal.
	deg^{-1} mole ⁻¹

This entropy value should be of use in determining the entropy of the periodate ions when the additional thermodynamic data are available.

Nature of the Transition.—The entropy change for the transition in Ag₂H₃IO₆ may be calculated if the reasonable assumption is made that the hydrogen bond arrangement is similar to that in the corresponding ammonium salt. The octahedral IO₆ ion is linked to neighboring paraperiodate groups by six hydrogen bonds: that is, one hydrogen lies along each oxygen-oxygen line connecting the IO₆ groups and this hydrogen is closer to one oxygen than to the other. These bonds are not symmetrically ordered about the central group as in the case of ice, and hence the bonds are not of equal energy. A rearrangement of the hydrogen bonds to some preferred orientation of lowest energy is therefore possible at not too low a temperature. The total number of protons adjacent to a paraperiodate group is restricted to three by electrostatic considerations.

The entropy change from an oriented to a random arrangement of the hydrogens may be calculated by the method used by Pauling⁴ for ice. If W is the number of accessible configurations, $\Delta S = Nk \ln W$. In a mole of Ag₂H₈IO₆ there are 3 N hydrogens, and if each hydrogen had a possibility of two positions, the total number of configurations would be 2^{3N} . However, many of these configurations are forbidden by the restriction that only three hydrogens may be near a paraperiodate ion. This reduces the total number of accessible configurations to $(20/64)^{N}2^{3N}$ or $(5/2)^{N}$

and the theoretical entropy change, ΔS , is R in 5/2 = 1.82 cal. mole⁻¹ deg.⁻¹.

If, however, the method of Slater⁸ or Onsager¹⁸ is followed, which takes into account the fact that all the allowed positions of the hydrogen atoms do not have the same energy, the following partition function for the states above the Curie point can be set up

$$Z = 2^{3N} \left[\frac{2}{64} e^{-\epsilon/kT} + \frac{18}{64} e^{-\epsilon/kT} \right]^N = \left(\frac{1}{4} + \frac{9}{4} e^{-\epsilon/kT} \right)^N$$

In this equation, the twenty allowed states of the sixty-four are distinguished by assuming that eighteen have an energy e higher than the two of zero energy. Below the Curie point all the dipoles are assumed to be parallel to the axis, hence Z = 1. The theoretical entropy change, ΔS , calculated in this manner, is $3/4 R \ln 3$ or 1.64 e. u., and at infinite temperatures $\Delta S = R \ln 5/2$, in agreement with the value obtained by employing Pauling's method. Thus the results of this research seem to indicate an entropy change associated with the transition of $3/4 R \ln 3$, which makes itself evident in a relatively small temperature range around the transition temperature. This entropy change probably increases slowly with increasing temperature until it reaches the value $R \ln 5/2$ at high temperatures.

Table IV

Substance	Transition temperature, T, °K.	ΔH , cal. mole ⁻¹	۵۲, cal. deg1 mole1
$\rm KH_2PO_4$	121.97 ± 0.05	87 ± 6	0.74 ± 0.06
KH2AsO4	95.57 ± 0.05	84 ± 4	0.90 ± 0.05
NH₄H₂PO₄	147.9 ± 1.0	154 ± 5	1.05 ± 0.04
NH4H2AsO4	216.1 ± 0.5	220 ± 15	1.02 ± 0.07
$Ag_2H_3IO_6$	227.25 ± 0.2	358 ± 20	1.60 ± 0.10

For convenience, the entropy changes, heats of transition and transition temperatures for the five similar substances are summarized in Table IV. The theoretical entropy change for the dihydrogen

(18) Onsager, presented at Conference on Dielectrics, New York Academy of Sciences, May, 1939. phosphates and arsenates is 0.69 increasing to a total change of 0.81 cal. deg.⁻¹ mole⁻¹. These results agree as well as can be expected with the predictions of theory, and justify the assumptions of the hydrogen bond theory. In view of the fact that the entropy calculation is made for constant pressure rather than constant volume, and that an arbitrary "normal" heat capacity is assumed, the results cannot be used to determine whether the total theoretical entropy change occurs in a relatively narrow temperature interval. In the case of silver trihydrogen paraperiodate the calculations following the method of Slater and Onsager give better agreement. The higher results for the ammonium salts may be explained by an entropy contribution above the theoretical value caused by abnormal volume changes at the transition.

The calculated entropies of transition have been confirmed in these cases, and the same theory may be applied with confidence to other substances when the hydrogen bond arrangement is known in sufficient detail. In addition, these results may be considered as additional evidence for the interpretation of the residual entropies of ice and heavy ice, where the transition is not observed.

Summary

The heat capacity of silver trihydrogen paraperiodate has been measured from 15 to 300°K. A region of abnormally high heat capacity occurs between 180 and 270°K., and the maximum in the heat capacity curve is at 227.25 \pm 0.20°K. The change in heat content for this non-isothermal transition is 358.1 \pm 20.0 cal. mole⁻¹ and the corresponding entropy change is 1.60 \pm 0.10 cal. mole⁻¹ deg.⁻¹.

The entropy change agrees within the limits of error with the calculated value of $3/4 R \ln 3$ or $1.64 \text{ cal. mole}^{-1} \text{ deg.}^{-1}$, based on a hydrogen bond theory of the transition.

The entropy of crystalline $Ag_2H_3IO_6$ at 298.19°K. is 59.44 = 0.10 cal. deg.⁻¹ mole⁻¹. CAMBRIDGE, MASS. RECEIVED APRIL 21, 1944

[CONTRIBUTION FROM THE DIVISION OF PLANT NUTRITION, COLLEGE OF AGRICULTURE, AND THE DEPARTMENT OF BAC-TERIOLOGY, UNIVERSITY OF CALIFORNIA]

Enzymatically Synthesized Crystalline Sucrose

BY W. Z. HASSID, M. DOUDOROFF AND H. A. BARKER

Doudoroff, et al., ^{1,2} have shown recently that the bacterium *Pseudomonas saccharophila* Doudoroff contains a sucrose phosphorylase catalyzing the reaction: sucrose + inorganic phosphate \rightarrow glucose-1-phosphate + fructose. Evidence was obtained indicating the reaction to be reversible: in the presence of purified phosphorylase, fructose and glucose-1-phosphate react to give inorganic phos-

(1) M. Doudoroff, N. Kaplan and W. Z. Hassid, J. Biol. Chem., 148, 67 (1943).

(2) M. Doudoroff, ibid.; 151, 351 (1943).

phate and a carbohydrate having certain properties of sucrose. The data previously reported are not, however, sufficient to justify the conclusion that the product of the reverse reaction is identical with natural sucrose. Further work was, therefore, undertaken to isolate and positively identify the synthetic product. The results here reported show conclusively that the synthetic product is sucrose.

There is some uncertainty as to whether or not sucrose has been previously synthesized. Pictet